

中國科學院高能物理研究所

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Chiral quark model for meson production in the resonance region

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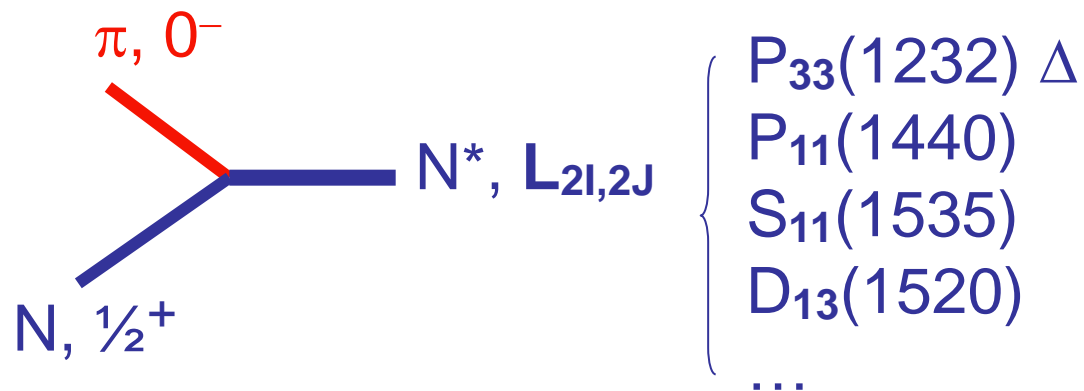
MENU2010, June 01, 2010, Williamsburg

Outline

- ◆ The “missing baryon resonances” problem
- ◆ Effective chiral Lagrangian for quark-pseudoscalar-meson interaction
- ◆ Baryon resonances in pseudoscalar meson photoproduction and meson-nucleon scatterings
- ◆ Prospects

1. “Missing baryon resonances in πN scattering

- The non-relativistic constituent quark model (NRCQM) makes great success in the description of hadron spectroscopy:
meson ($q \bar{q}$), baryon (qqq).
- However, it also predicted a much richer baryon spectrum, where some of those have not been seen in πN scatterings.
 - “Missing Resonances”.



PDG2008: 22 nucleon resonances (uud, udd)

Particle	$L_{2I \cdot 2J}$	Overall status	Status as seen in —						
			$N\pi$	$N\eta$	ΛK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$
$N(939)$	P_{11}	****							
$N(1440)$	P_{11}	****	****	*			***	*	***
$N(1520)$	D_{13}	****	****	*			*****	*****	*****
$N(1535)$	S_{11}	****	****	*****			*	**	***
$N(1650)$	S_{11}	****	****	*	***	**	***	**	***
$N(1675)$	D_{15}	****	****	*	*		*****	*	*****
$N(1680)$	F_{15}	****	****				*****	*****	*****
$N(1700)$	D_{13}	***	***	*	**	*	**	*	**
$N(1710)$	P_{11}	***	***	**	**	*	**	*	***
$N(1720)$	P_{13}	****	****	*	**	*	*	**	**
$N(1900)$	P_{13}	**	**					*	
$N(1990)$	F_{17}	**	**	*	*	*			*
$N(2000)$	F_{15}	**	**	*	*	*	*	**	
$N(2080)$	D_{13}	**	**	*	*				*
$N(2090)$	S_{11}	*	*						
$N(2100)$	P_{11}	*	*	*					
$N(2190)$	G_{17}	****	****	*	*	*		*	*
$N(2200)$	D_{15}	**	**	*	*				
$N(2220)$	H_{19}	****	****	*					
$N(2250)$	G_{19}	****	****	*					
$N(2600)$	I_{111}	***	***						
$N(2700)$	K_{113}	**	**						

(**)
not well-
established

Dilemma:

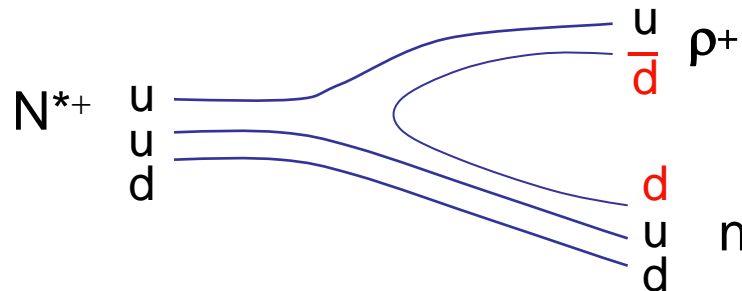
a) The NRCQM is **WRONG**: quark-diquark configuration? ...



b) The NRCQM is **CORRECT**, but those missing states have only weak couplings to πN , i.e. small $g_{\pi N^* N}$. (Isgur, 1980)

Looking for “missing resonances” in $N^* \rightarrow \eta N, K\Sigma, K\Lambda, \rho N, \omega N, \phi N, \gamma N \dots$

(Exotics ...)



Questions:

Should we take the naïve quark model seriously?

How far one can go with it?

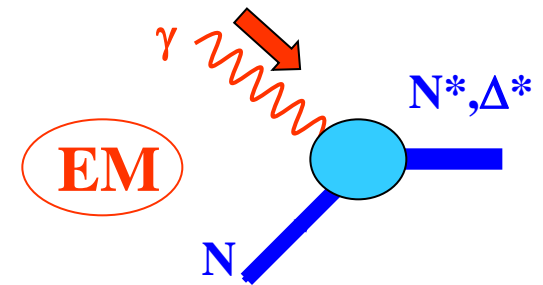
What is the success and what is the failure?

... ..

□ The first orbital excitation states in the NRCQM

Existing features with the first orbital excitation states:

- i) In the light quark sector, the NRCQM allows the groundstate $[56, {}^2_8]$ (p and n) to be excited to $[70, {}^2_8]$ and $[70, {}^4_8]$ octets, and $[70, {}^2_{10}]$ decuplet via single photon absorption.



$$|70, {}^2_8, 1, 1, J\rangle \quad \bullet \quad S_{11}(1535) \text{ (****)}, D_{13}(1520) \text{ (****)}$$

$$|70, {}^4_8, 1, 1, J\rangle \quad \bullet \quad S_{11}(1650) \text{ (****)}, D_{13}(1700) \text{ (***)}, D_{15}(1675) \text{ (****)}$$

$$|70, {}^2_{10}, 1, 1, J\rangle \quad \bullet \quad S_{31}(1620) \text{ (****)}, D_{33}(1670) \text{ (****)}$$

$$|70, {}^2_1, 1, 1, J\rangle \quad \bullet \quad \Lambda(1405) S_{01} \text{ (****)}, \Lambda(1520) D_{03} \text{ (***)}$$

The $SU(6) \otimes O(3)$ symmetry must be broken due to spin-dependent forces. Thus, state mixings are inevitable.

Several NRCQM selection rules are violated:

- **Moorhouse selection rule** (Moorhouse, PRL16, 771 (1966))

$$\begin{aligned}\gamma + p(|56, {}^28; 0, 0, 1/2\rangle) &\not\leftrightarrow N^*(|70, {}^48\rangle) \\ \gamma + n(|56, {}^28; 0, 0, 1/2\rangle) &\leftrightarrow N^*(|70, {}^48\rangle)\end{aligned}$$

- **Λ selection rule** (Zhao & Close, PRD74, 094014(2006)) in strong decays

$$N^*(|70, {}^48\rangle) \not\leftrightarrow K(K^*) + \Lambda$$

- **Faiman-Hendry selection rule** (Faiman & Hendry, PR173, 1720 (1968)).

$$\Lambda^*(|70, {}^48\rangle) \not\leftrightarrow N(|56, {}^28; 0, 0, 1/2\rangle) + \bar{K}$$

2. Effective chiral Lagrangian for quark-pseudoscalar meson interactions

For pion photoproduction, the low energy theorem (LET) provides a crucial test near threshold. In order to recover the LET, one has to rely on the low energy QCD Lagrangian which keeps the meson-baryon interaction invariant under the chiral transformation. Combining the low energy QCD Lagrangian with the quark model, we introduce the quark-meson interaction through the effective Lagrangian:

$$\mathcal{L} = \bar{\psi}[\gamma_{\mu}(i\partial^{\mu} + V^{\mu} + \gamma_5 A^{\mu}) - m]\psi + \dots,$$

where the vector and axial currents are

$$\begin{aligned} V_{\mu} &= \frac{1}{2}(\xi^{\dagger}\partial_{\mu}\xi + \xi\partial_{\mu}\xi^{\dagger}), \\ A_{\mu} &= i\frac{1}{2}(\xi^{\dagger}\partial_{\mu}\xi - \xi\partial_{\mu}\xi^{\dagger}), \end{aligned}$$

A. Manohar and H. Georgi, Nucl. Phys. **B234**, 189 (1984).

and the chiral transformation is,

$$\xi = e^{i\phi_m/f_m}, \quad (77)$$

where f_m is the decay constant of the meson. The quark field ψ in the SU(3) symmetry is

$$\psi = \begin{pmatrix} \psi(u) \\ \psi(d) \\ \psi(s) \end{pmatrix}, \quad (78)$$

and the meson field ϕ_m is a $3 \otimes 3$ matrix:

$$\phi_m = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}, \quad (79)$$

where the pseudoscalar mesons π , η and K are treated as Goldstone bosons. Thus, the Lagrangian in Eq. (121) is invariant under the chiral transformation. Expanding the nonlinear field ξ in Eq. (77) in terms of the Goldstone boson field ϕ_m , i.e. $\xi = 1 + i\phi_m/f_m + \dots$, we obtain the standard quark-meson pseudovector coupling at tree level:

$$H_m = \sum_j \frac{1}{f_m} \bar{\psi}_j \gamma_\mu^j \gamma_5^j \psi_j \partial^\mu \phi_m, \quad (80)$$

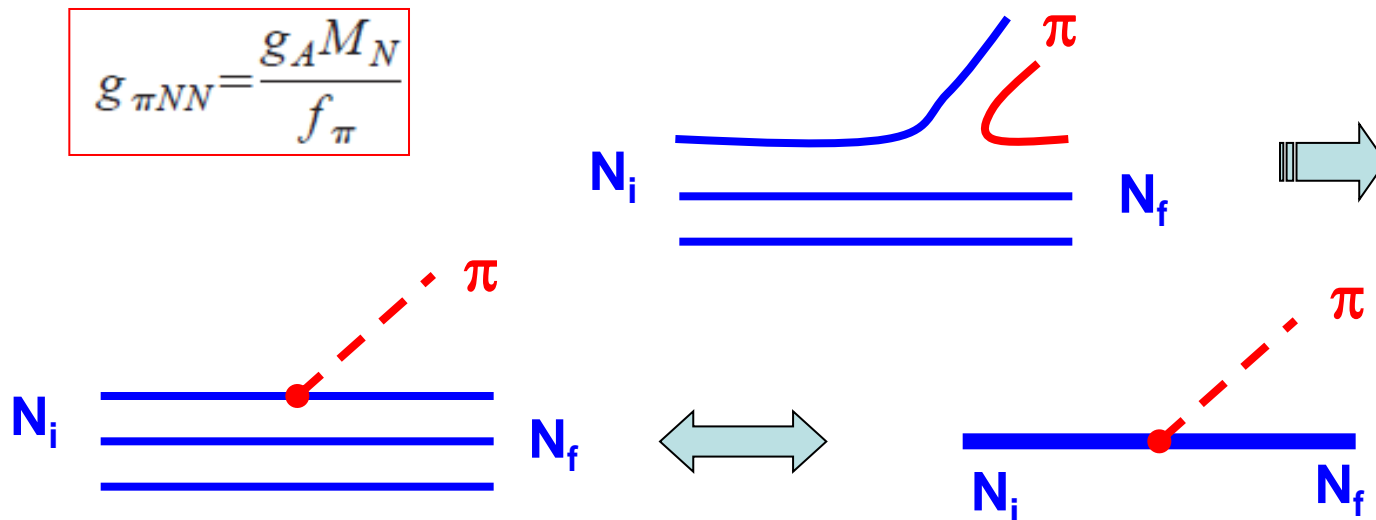
where ψ_j ($\bar{\psi}_j$) represents the j th quark (anti-quark) field in the nucleon.

Test of Goldberger-Treiman relation:

Note that, g_A , the axial vector coupling, relates the hadronic operator σ to the quark operator σ_j for the j -th quark, and is defined by

$$\langle N_f | \sum_j \hat{I}_j \sigma_j | N_i \rangle \equiv g_A \langle N_f | \sigma | N_i \rangle.$$

To equate the quark-level coupling to the hadronic level one for the πNN vertex, i.e. axial current conservation, one has



□ Baryon excitations in $\pi^- p \rightarrow \eta n$

The process $\pi^- p \rightarrow \eta n$ can be expressed in term of the Mandelstam variables:

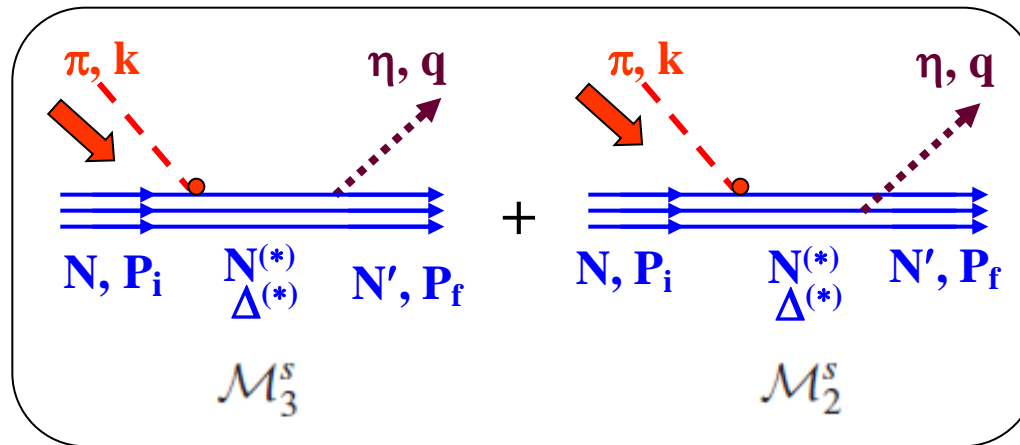
$$\mathcal{M} = \mathcal{M}_s + \mathcal{M}_u + \mathcal{M}_t.$$

The s - and u -channel transitions are given by

$$\mathcal{M}_s = \sum_j \langle N_f | H_\eta | N_j \rangle \langle N_j | \frac{1}{E_i + \omega_\pi - E_j} H_\pi | N_i \rangle$$
$$\mathcal{M}_u = \sum_j \langle N_f | H_\pi \frac{1}{E_i - \omega_\eta - E_j} | N_j \rangle \langle N_j | H_\eta | N_i \rangle.$$

Zhong, Zhao, He, and Saghai, PRC76, 065205 (2007);
Zhong and Zhao, Phys. Rev. C 79, 045202 (2009)

s-channel



$$\mathcal{M}_s = \sum_j \langle N_f | H_\eta | N_j \rangle \langle N_j | \sum_n \frac{1}{\omega_\pi^{n+1}} (\hat{H} - E_i)^n H_\pi | N_i \rangle$$

for any operator \mathcal{O} , one has

$$(\hat{H} - E_i) \mathcal{O} | N_i \rangle = [\hat{H}, \mathcal{O}] | N_i \rangle$$

Refs.

Zhao, Li, & Bennhold, PLB436, 42(1998); PRC58, 2393(1998);

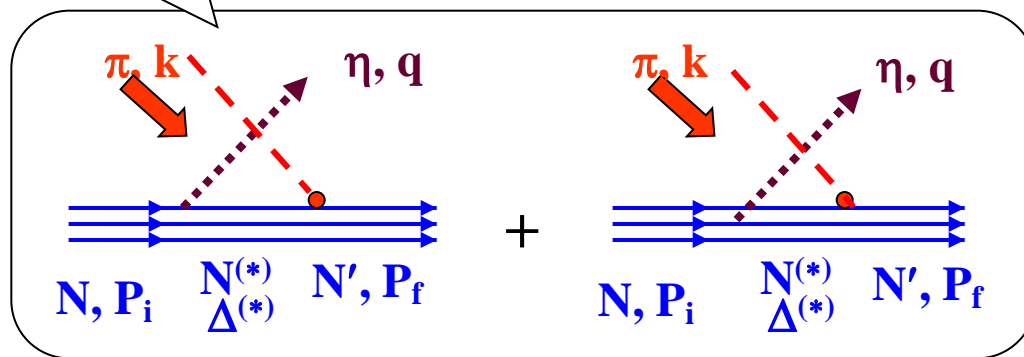
Zhao, Didelez, Guidal, & Saghai, NPA660, 323(1999);

Zhao, PRC63, 025203(2001);

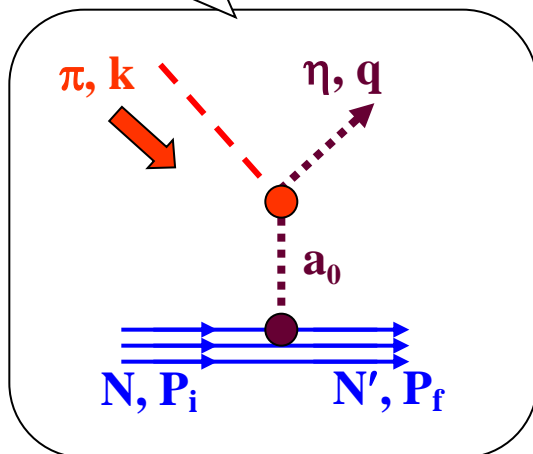
Zhao, Saghai, Al-Khalili, PLB509, 231(2001);

Zhao, Al-Khalili, & Bennhold, PRC64, 052201(R)(2001); PRC65, 032201(R) (2002);

u-channel



t-channel



$$\left\{ \begin{array}{l} \mathcal{L}_{a_0\pi\eta} = g_{a_0\pi\eta} m_\pi \eta \vec{\pi} \vec{a}_0 \\ H_{a_0} = \sum_j g_{a_0qq} m_\pi \bar{\psi}_j \psi_j \vec{a}_0 \end{array} \right.$$

$$\mathcal{M}_t = g_{a_0\pi\eta} m_\pi \langle N_f | H_{a_0} | N_i \rangle \frac{1}{t^2 - m_{a_0}^2}$$

◆ S-channel transition amplitude with quark level operators

Non-relativistic expansion:

$$H_{\pi} = \sum_j \frac{I_j}{g_A^{\pi}} \boldsymbol{\sigma}_j \cdot \left[\mathbf{A}_{\pi} e^{i\mathbf{k} \cdot \mathbf{r}_j} + \frac{\omega_{\pi}}{2m_q} \{ \mathbf{p}_j, e^{i\mathbf{k} \cdot \mathbf{r}_j} \} \right],$$

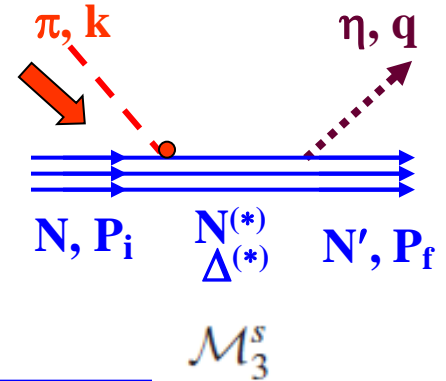
$$H_{\eta} = \sum_j \frac{I_j}{g_A^{\eta}} \boldsymbol{\sigma}_j \cdot \left[\mathbf{A}_{\eta} e^{-i\mathbf{q} \cdot \mathbf{r}_j} + \frac{\omega_{\eta}}{2m_q} \{ \mathbf{p}_j, e^{-i\mathbf{q} \cdot \mathbf{r}_j} \} \right],$$

with

$$\mathbf{A}_{\pi} = - \left(\frac{\omega_{\pi}}{E_i + M_i} + 1 \right) \mathbf{k},$$

$$\mathbf{A}_{\eta} = - \left(\frac{\omega_{\eta}}{E_f + M_f} + 1 \right) \mathbf{q}.$$

$$\mathcal{M}^s = \sum_n (\mathcal{M}_3^s + \mathcal{M}_2^s) e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2}$$

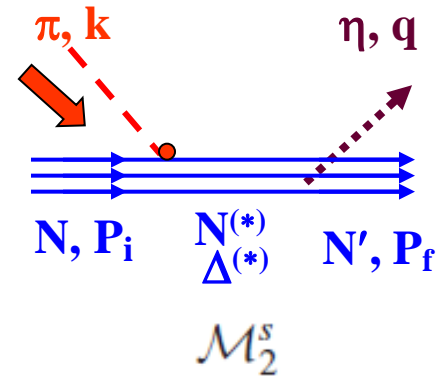


with

$$\begin{aligned} \mathcal{M}_3^s = & \langle N_f | \frac{3I_3}{g_A^\pi} \left\{ \sigma_3 \cdot \mathbf{A}_\eta \sigma_3 \cdot \mathbf{A}_\pi \sum_{n=0} \frac{F_s(n)}{n!} \mathcal{X}^n \right. \\ & + \left[-\sigma_3 \cdot \mathbf{A}_\eta \frac{\omega_\pi}{3m_q} \sigma_3 \cdot \mathbf{q} - \frac{\omega_\eta}{3m_q} \sigma_3 \cdot \mathbf{k} \sigma_3 \cdot \mathbf{A}_\pi \right. \\ & \left. \left. + \frac{\omega_\eta}{m_q} \frac{\omega_\pi}{m_q} \frac{\alpha^2}{3} \right] \sum_{n=1} \frac{F_s(n)}{(n-1)!} \mathcal{X}^{n-1} \right. \\ & \left. + \frac{\omega_\eta}{3m_q} \frac{\omega_\pi}{3m_q} \sigma_3 \cdot \mathbf{q} \sigma_3 \cdot \mathbf{k} \sum_{n=2} \frac{F_s(n)}{(n-2)!} \mathcal{X}^{n-2} \right\} |N_i\rangle \end{aligned}$$

where $\mathcal{X} \equiv \mathbf{k} \cdot \mathbf{q}/3\alpha^2$.

$$\mathcal{M}^s = \sum_n (\mathcal{M}_3^s + \mathcal{M}_2^s) e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2}$$



with

$$\mathcal{M}_3^s = \langle N_f | \frac{3I_3}{g_A^\pi} \left\{ \sigma_3 \cdot \mathbf{A}_\eta \sigma_3 \cdot \mathbf{A}_\pi \sum_{n=0} \frac{F_s(n)}{n!} \chi^n \right.$$

$$\begin{aligned} \mathcal{M}_2^s = \langle N_f | \frac{6I_1}{g_A^\pi} \left\{ \sigma_1 \cdot \mathbf{A}_\eta \sigma_3 \cdot \mathbf{A}_\pi \sum_{n=0} \frac{F_s(n)}{n!} \frac{\chi^n}{(-2)^n} \right. \\ + \left[-\sigma_1 \cdot \mathbf{A}_\eta \frac{\omega_\pi}{3m_q} \sigma_3 \cdot \mathbf{q} - \frac{\omega_\eta}{3m_q} \sigma_1 \cdot \mathbf{k} \sigma_3 \cdot \mathbf{A}_\pi \right. \\ \left. \left. + \frac{\omega_\eta}{m_q} \frac{\omega_\pi}{m_q} \frac{\alpha^2}{3} \sigma_1 \cdot \sigma_3 \right] \sum_{n=1} \frac{F_s(n)}{(n-1)!} \frac{\chi^{n-1}}{(-2)^n} \right. \end{aligned}$$

where

$$\left. + \frac{\omega_\eta}{3m_q} \frac{\omega_\pi}{3m_q} \sigma_1 \cdot \mathbf{q} \sigma_3 \cdot \mathbf{k} \sum_{n=2} \frac{F_s(n)}{(n-2)!} \frac{\chi^{n-2}}{(-2)^n} \right\} |N_i\rangle$$

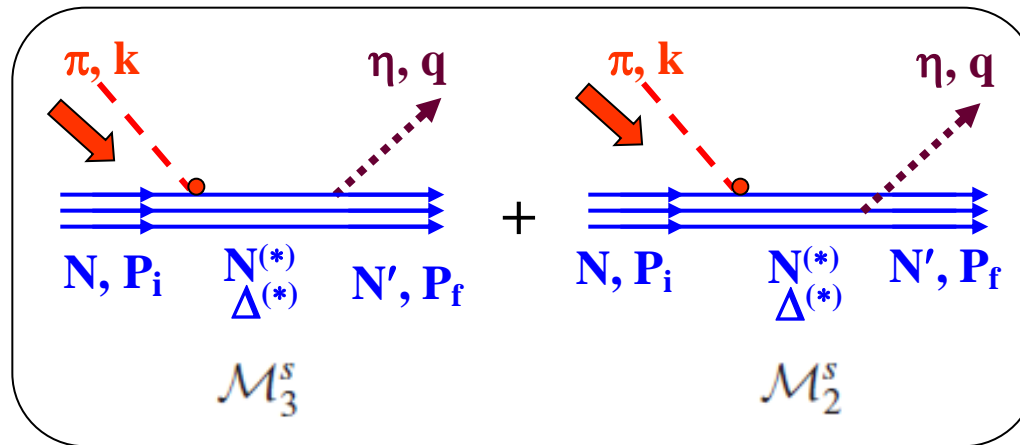
◆ quark level → hadron level

$$\begin{aligned}
 \mathcal{M}^s = & \frac{1}{g_A^\pi} \left\{ \mathbf{A}_\eta \cdot \mathbf{A}_\pi \sum_{n=0} [g_{s1} + (-2)^{-n} g_{s2}] \frac{F_s(n)}{n!} \chi^n \right. \\
 & + \left(-\frac{\omega_\pi}{3m_q} \mathbf{A}_\eta \cdot \mathbf{q} - \frac{\omega_\eta}{3m_q} \mathbf{A}_\pi \cdot \mathbf{k} + \frac{\omega_\eta}{m_q} \frac{\omega_\pi}{m_q} \frac{\alpha^2}{3} \right) \\
 & \times \sum_{n=1} [g_{s1} + (-2)^{-n} g_{s2}] \frac{F_s(n)}{(n-1)!} \chi^{n-1} \\
 & + \frac{\omega_\eta \omega_\pi}{(3m_q)^2} \mathbf{k} \cdot \mathbf{q} \sum_{n=2} \frac{F_s(n)}{(n-2)!} [g_{s1} + (-2)^{-n} g_{s2}] \\
 & + i \boldsymbol{\sigma} \cdot (\mathbf{A}_\eta \times \mathbf{A}_\pi) \sum_{n=0} [g_{v1} + (-2)^{-n} g_{v2}] \frac{F_s(n)}{n!} \chi^n \\
 & + \frac{\omega_\eta \omega_\pi}{(3m_q)^2} i \boldsymbol{\sigma} \cdot (\mathbf{q} \times \mathbf{k}) \\
 & \left. \times \sum_{n=2} [g_{v1} + (-2)^{-n} g_{v2}] \frac{F_s(n)}{(n-2)!} \chi^{n-2} \right\} e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2}
 \end{aligned}$$

$$F_s(n) = \frac{M_n}{P_i \cdot k - n M_n \omega_h}$$

$$\rightarrow F_s(R) = \frac{2M_R}{s - M_R^2 + i M_R \Gamma_R}$$

s-channel



- Compared with M_3^s , amplitude M_2^s is relatively suppressed by a factor of $(-1/2)^n$ for each n .
- Higher excited states are relatively suppressed by $(k \cdot q / 3\alpha^2)^n / n!$
- One can identify the quark motion correlations between the initial and final state baryon
- Similar treatment can be done for the u channel

◆ Separate out individual resonances

A. $n = 0$ shell resonances

For $n = 0$, only the nucleon pole term contributes to the transition amplitude. Its s -channel amplitude is

$$\mathcal{M}_N^s = \mathcal{O}_N \frac{2M_0}{s - M_0^2} e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2},$$

with

$$\mathcal{O}_N = [g_{s1} + g_{s2}] \mathbf{A}_\eta \cdot \mathbf{A}_\pi + [g_{v1} + g_{v2}] i\boldsymbol{\sigma} \cdot (\mathbf{A}_\eta \times \mathbf{A}_\pi),$$

where M_0 is the nucleon mass.

B. $n = 1$ shell resonances

For $n = 1$, only S and D waves contribute in the s channel. Note that the spin-independent amplitude for D waves is proportional to the Legendre function $P_2^0(\cos \theta)$ and the spin-dependent amplitude for D waves is in proportion to $\frac{\partial}{\partial \theta} P_2^0(\cos \theta)$. Moreover, the S -wave amplitude is independent of the scattering angle.

$$\begin{aligned}\mathcal{M}^s(S) &= \mathcal{O}_S F_s(R) e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2}, \\ \mathcal{M}^s(D) &= \mathcal{O}_D F_s(R) e^{-(\mathbf{k}^2 + \mathbf{q}^2)/6\alpha^2},\end{aligned}$$

with

$$\begin{aligned}\mathcal{O}_S &= \left(g_{s1} - \frac{1}{2} g_{s2} \right) \left(|\mathbf{A}_\eta| |\mathbf{A}_\pi| \frac{|\mathbf{k}| |\mathbf{q}|}{9\alpha^2} - \frac{\omega_\pi}{3m_q} \mathbf{A}'_\eta \cdot \mathbf{q} \right. \\ &\quad \left. - \frac{\omega_\eta}{3m_q} \mathbf{A}_\pi \cdot \mathbf{k} + \frac{\omega_\eta}{m_q} \frac{\omega_\pi}{m_q} \frac{\alpha^2}{3} \right), \\ \mathcal{O}_D &= \left(g_{s1} - \frac{1}{2} g_{s2} \right) |\mathbf{A}_\eta| |\mathbf{A}_\pi| (3 \cos^2 \theta - 1) \frac{|\mathbf{k}| |\mathbf{q}|}{9\alpha^2} \\ &\quad + \left(g_{v1} - \frac{1}{2} g_{v2} \right) i \boldsymbol{\sigma} \cdot (\mathbf{A}_\eta \times \mathbf{A}_\pi) \frac{\mathbf{k} \cdot \mathbf{q}}{3\alpha^2}.\end{aligned}$$

$$\mathcal{M}^s(S) = [g_{S_{11}(1535)} + g_{S_{11}(1650)}]\mathcal{M}^s(S),$$

$$\mathcal{M}^s(D) = [g_{D_{13}(1520)} + g_{D_{13}(1700)} + g_{D_{15}(1675)}]\mathcal{M}^s(D).$$

In the SU(6) symmetry limit,

Factor	Value	Factor	Value	Factor	Value
g_{s1}	1	$g_{S_{11}(1535)}$	2	g_2	$5/3$
g_{s2}	$2/3$	$g_{S_{11}(1650)}$	-1	$g_{P_{11}(1710)}$	$180/619$
g_{v1}	$5/3$	$g_{D_{13}(1520)}$	2	$g_{P_{13}(1900)}$	$18/619$
g_{v2}	0	$g_{D_{13}(1700)}$	$-1/10$	$g_{P_{11}(2100)}$	$-16/619$
g_A^π	$5/3$	$g_{D_{15}(1675)}$	$-9/10$	$g_{F_{15}(1680)}$	$5/3$
g_A^η	1	$g_{P_{11}(1440)}$	$225/619$	$g_{F_{15}(2000)}$	$-2/21$
g_1	1	$g_{P_{13}(1720)}$	$180/619$	$g_{F_{17}(1990)}$	$-4/7$

◆ Model parameters

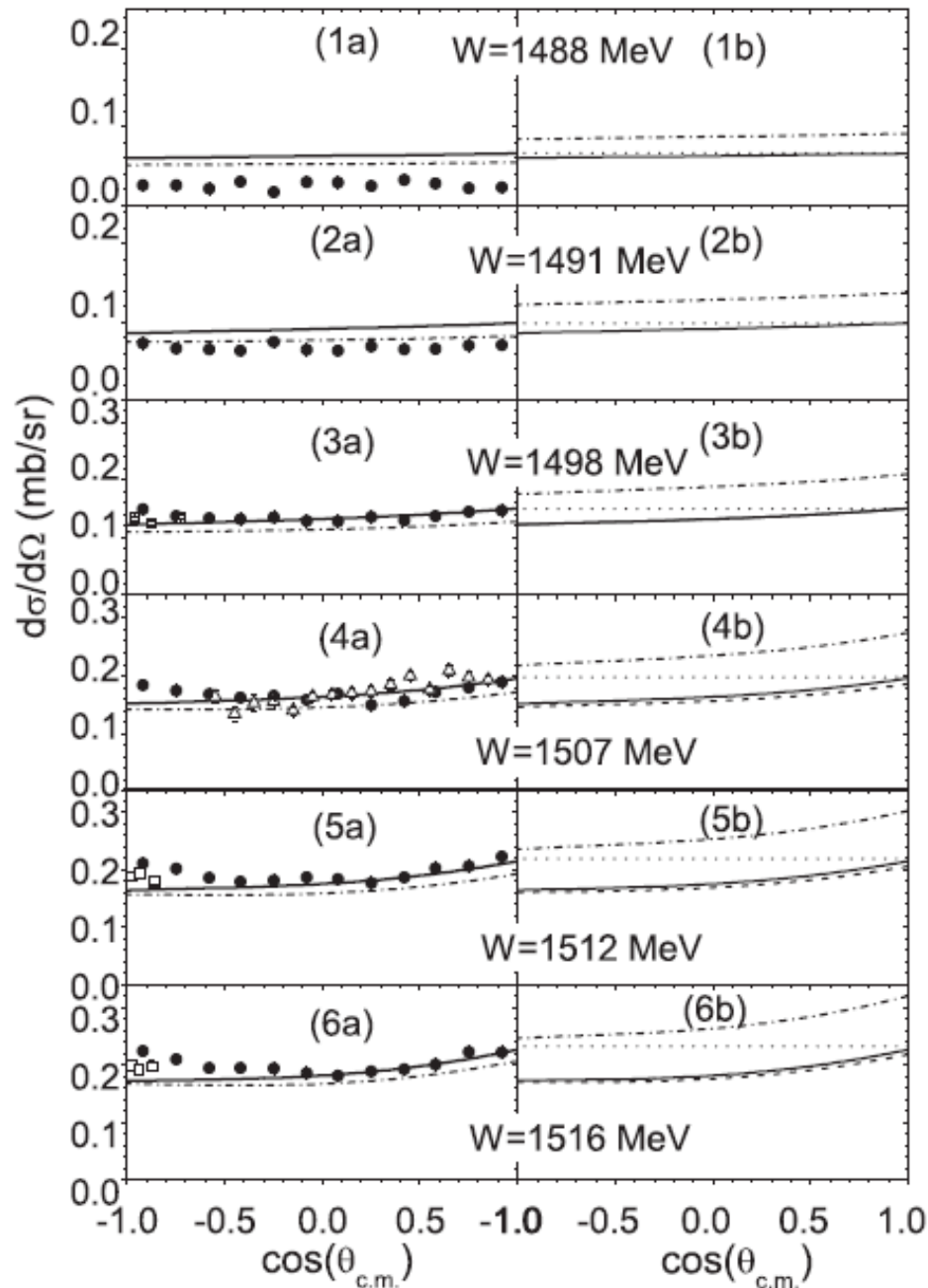
Goldberger-Treiman relation:

$$g_{mNN} = \frac{g_A^m M_N}{f_m}, \quad \begin{aligned} g_{\pi NN} &= 13.48, & m_q &= 330 \text{ MeV}, \\ g_{\eta NN} &= 0.81 & \alpha^2 &= 0.16 \text{ GeV}^2. \\ g_{a_0 NN} g_{a_0 \pi \eta} &= 100 \end{aligned}$$

TABLE II. Breit-Wigner masses M_R (in MeV) and widths Γ_R (in MeV) for the resonances. $n = 1$ and $n = 2$ stand for the degenerate states with quantum number $n = 1$ and $n = 2$ in the u channel.

Resonance	M_R	Γ_R	Resonance	M_R	Γ_R
$S_{11}(1535)$	1535	150	$P_{11}(1440)$	1440	300
$S_{11}(1650)$	1655	165	$P_{11}(1710)$	1710	100
$D_{13}(1520)$	1520	115	$P_{13}(1720)$	1720	200
$D_{13}(1700)$	1700	115	$P_{13}(1900)$	1900	500
$D_{15}(1675)$	1675	150	$P_{11}(2100)$	2100	150
$n = 1$	1650	230	$F_{15}(1680)$	1685	130
$n = 2$	1750	300	$F_{15}(2000)$	2000	200
—	—	—	$F_{17}(1990)$	1990	350

Differential cross sections

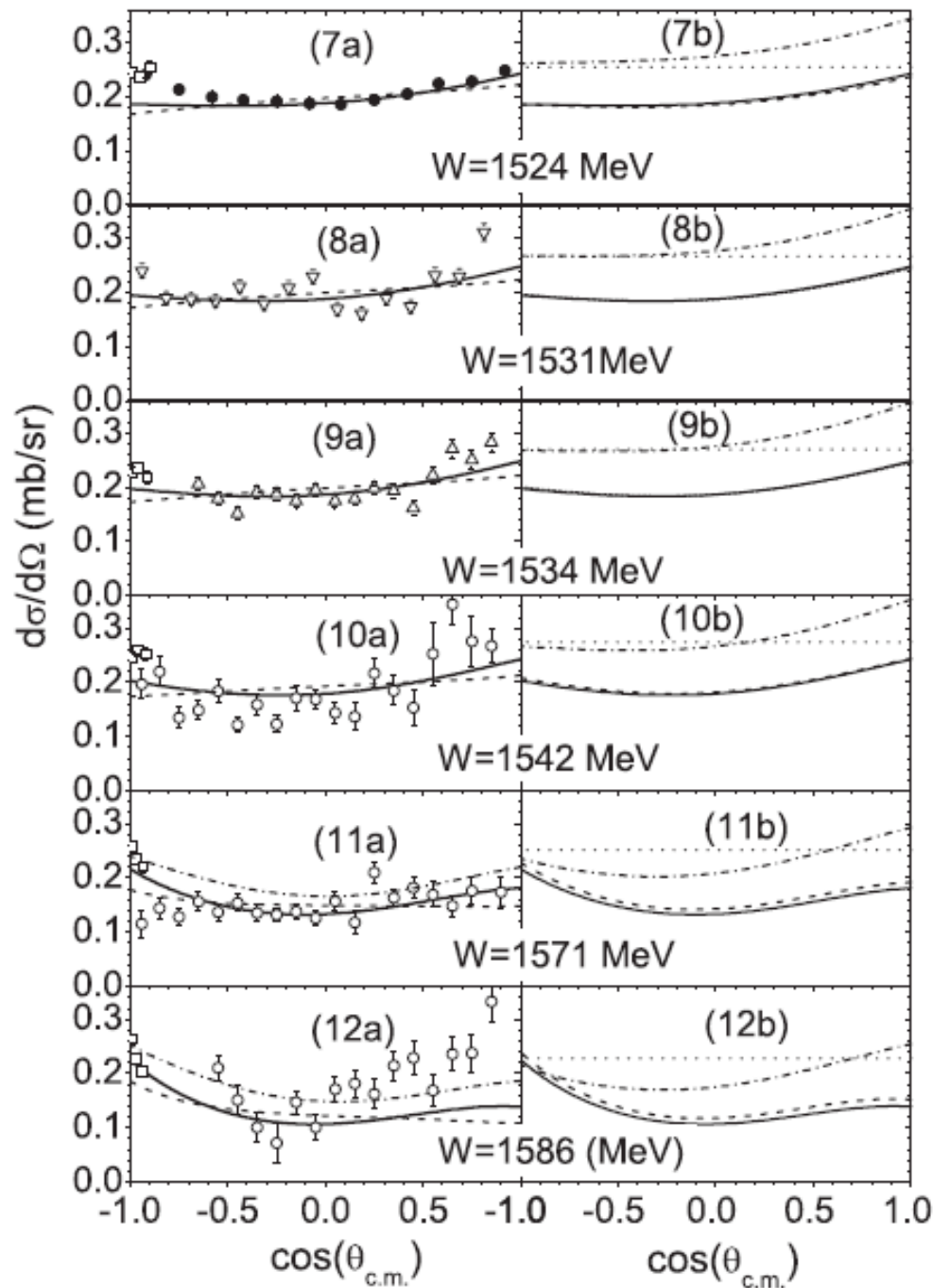


Left panel:

- Solid: full calculation
- Dot-dashed: without nucleon Born term

Right panel:

- Solid: full calculation
- Dotted lines: exclusive S11(1535)
- Dot-dashed: without S11(1650)
- Dashed: without t-channel



Left panel:

- Solid: full calculation
- Dot-dashed: without nucleon Born term
- Dashed: without D13(1520)

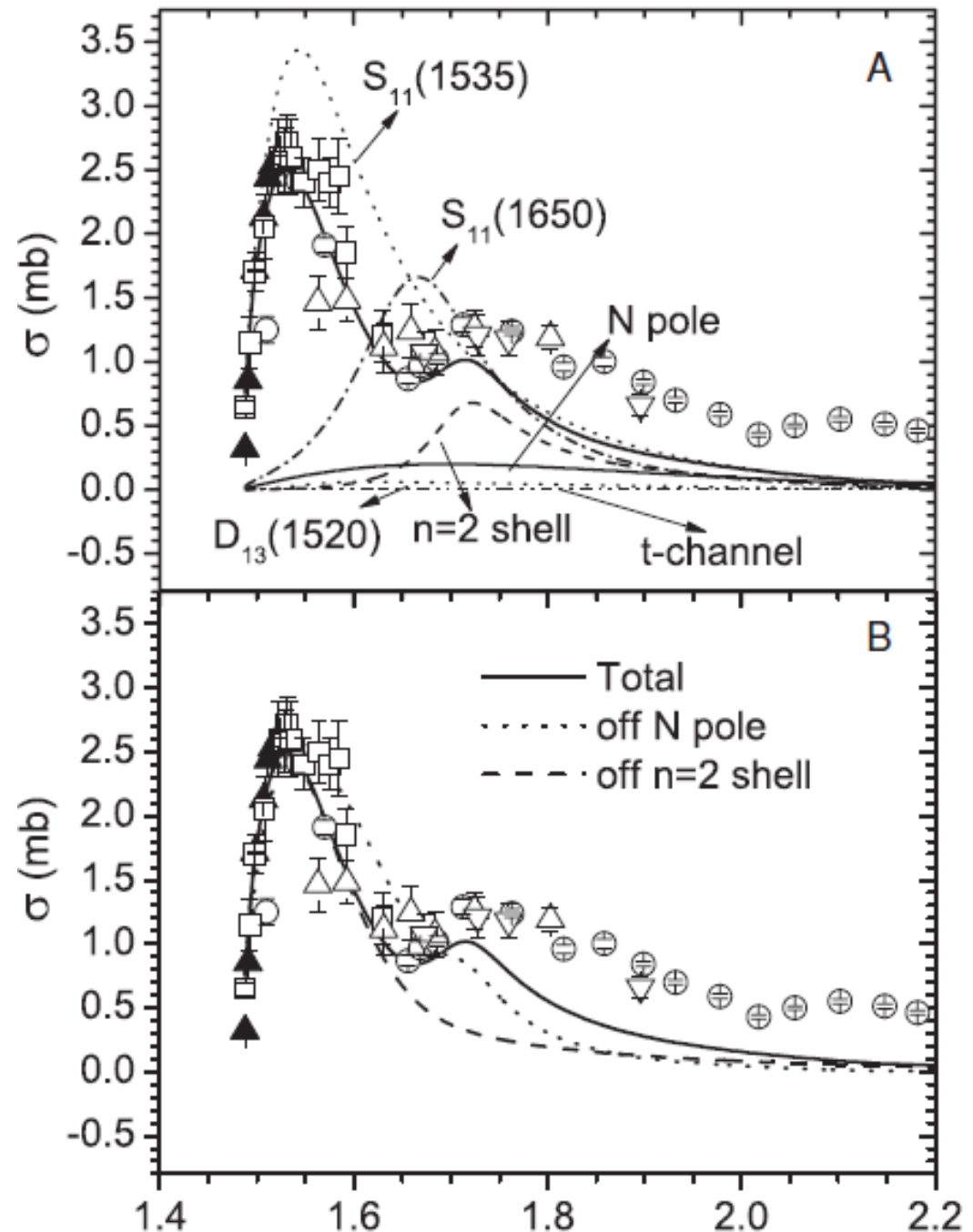
Right panel:

- Solid: full calculation
- Dotted lines: exclusive S11(1535)
- Dot-dashed: without S11(1650)
- Dashed: without t-channel

Total cross sections

- $S_{11}(1535)$ is dominant near threshold. The exclusive cross section is even larger than the data.
- $S_{11}(1650)$ has a destructive interference with the $S_{11}(1535)$, and appears to be a dip in the total cross section.
- States from $n=2$ shell account for the second enhancement around 1.7 GeV.

Zhong, Zhao, He, and Saghai,
PRC76, 065205 (2007)



□ S-channel resonance excitations in $K^-p \rightarrow \Sigma^0 \pi^0$

$$\mathcal{O}_S = [g_{S_{01}(1405)} + g_{S_{01}(1670)}]\mathcal{O}_S,$$

$$\mathcal{O}_D = [g_{D_{03}(1520)} + g_{D_{03}(1690)}]\mathcal{O}_D,$$

$$\frac{g_{S_{01}(1405)}}{g_{S_{01}(1670)}} = \frac{\langle N_f | I_3^\pi \sigma_3 | S_{01}(1405) \rangle \langle S_{01}(1405) | I_3^K \sigma_3 | N_i \rangle}{\langle N_f | I^\pi \sigma_3 | S_{01}(1670) \rangle \langle S_{01}(1670) | I_3^K \sigma_3 | N_i \rangle}$$

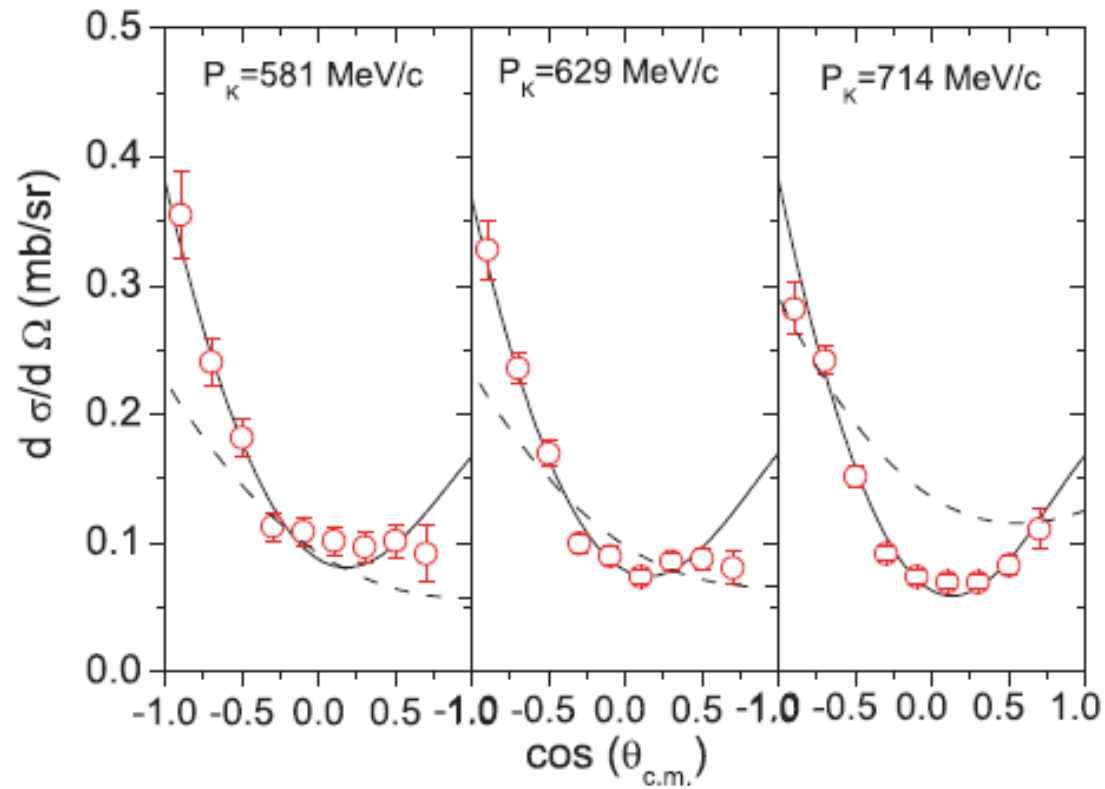
$$|S_{01}(1405)\rangle = \cos(\theta)|\mathbf{70},^2\mathbf{1}\rangle - \sin(\theta)|\mathbf{70},^2\mathbf{8}\rangle$$

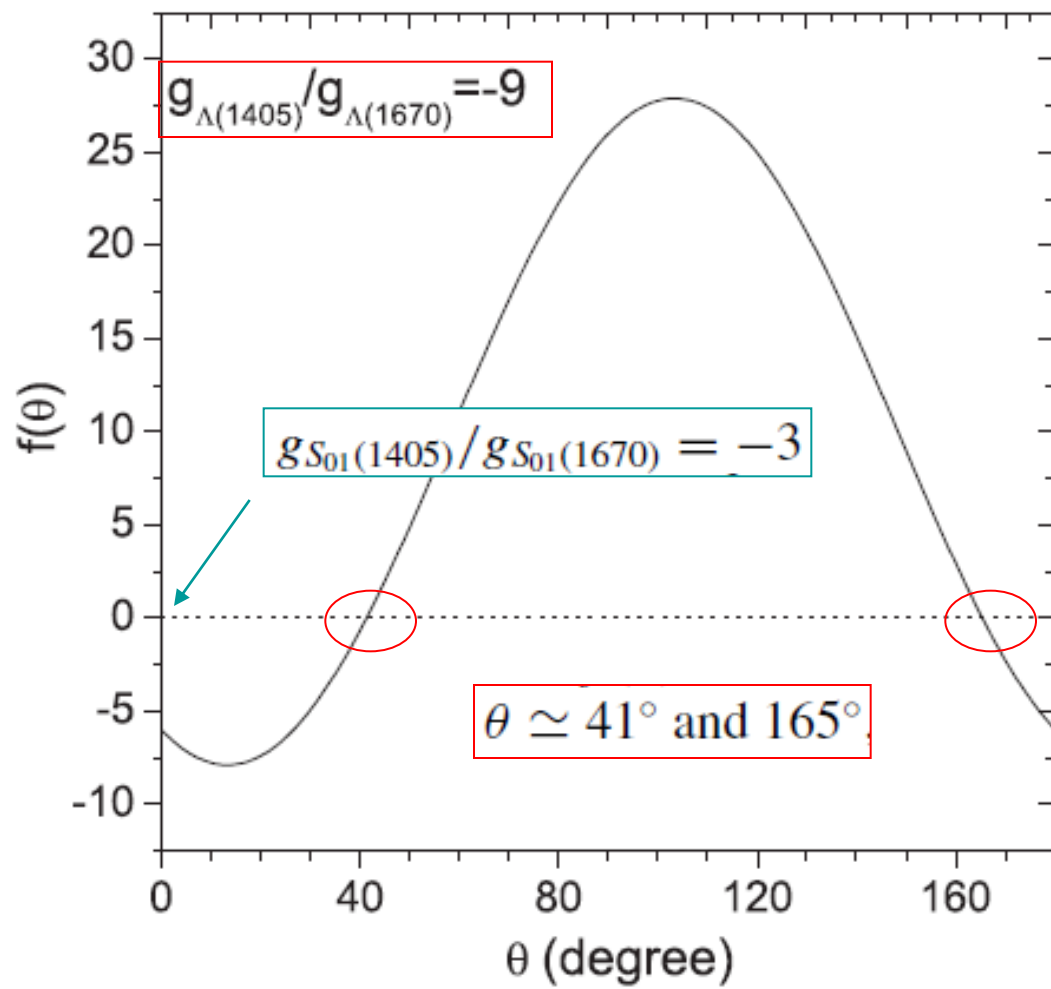
$$|S_{01}(1670)\rangle = \sin(\theta)|\mathbf{70},^2\mathbf{1}\rangle + \cos(\theta)|\mathbf{70},^2\mathbf{8}\rangle$$

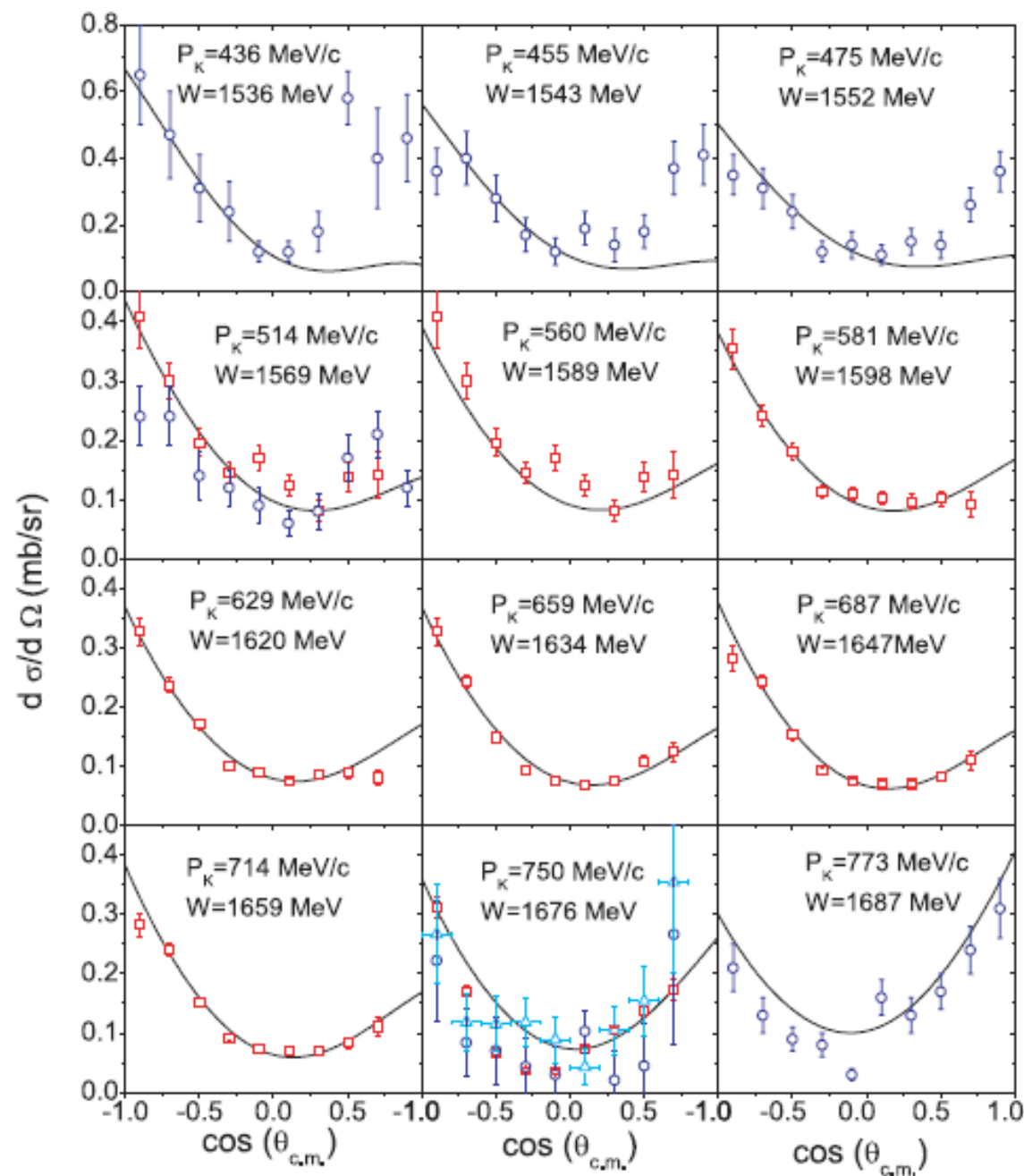
$$\frac{g_{S_{01}(1405)}}{g_{S_{01}(1670)}} = \frac{[3 \cos(\theta) - \sin(\theta)][\cos(\theta) + \sin(\theta)]}{[3 \sin(\theta) + \cos(\theta)][\sin(\theta) - \cos(\theta)]}$$

$g_{S_{01}(1405)}/g_{S_{01}(1670)} = -3$ leads to $\theta = 0^\circ$, i.e., no configuration mixing between $[\mathbf{70},^2\mathbf{1}]$ and $[\mathbf{70},^2\mathbf{8}]$.

We thus determine the mixing angle by experimental data which requires $g_{S_{01}(1405)}/g_{S_{01}(1670)} \simeq -9$







s-channel

$K^- (s \bar{u})$

\mathcal{M}_2^s

p

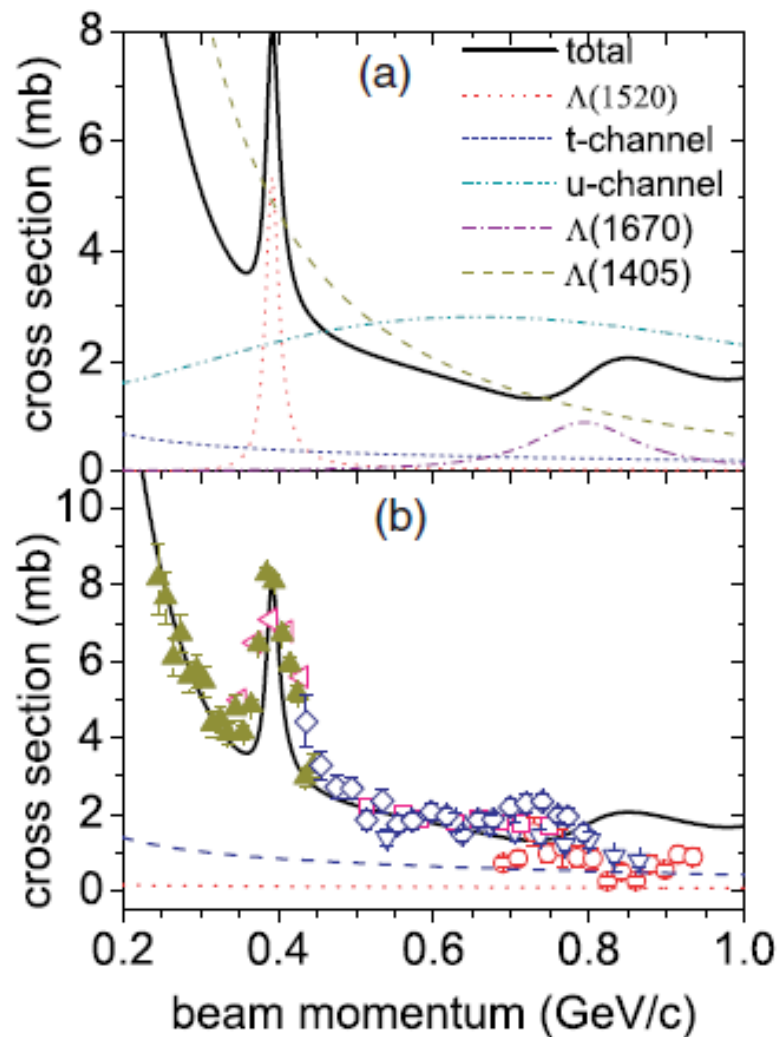
Σ

π

$\mathcal{M}_3^s = 0$

\mathcal{M}_2^s is the only s-channel amplitude

U-channel turns to be important



Prospects - I

1. For the purpose of searching for individual resonance excitations, it is essential to have a quark model guidance for both known and “missing” states. And then allow the data to tell:
 - i) which state is favored;
 - ii) whether a state beyond the conventional quark model is needed;
 - iii) how quark model prescriptions for N^*NM form factors complement with isobaric models.

Prospects - II

2. Understanding the non-resonance background

A reliable estimate of the non-resonance background, such as the t- and u-channel. Their interferences with the resonances are essentially important.

3. Unitarity constraint

A coherent study of the pseudoscalar photoproduction and meson-baryon scattering is needed. In particular, a coupled channel study will put a unitary constraint on the theory.

Photoproduction of pseudoscalar mesons (π , η , η' , K); and $\pi N \rightarrow \eta N$; $K^-p \rightarrow \pi\Sigma$, and more are coming out soon...

Q. Z., **PRC** **63**, 035205 (2001) ;

Q. Z., J.S. Al-Khalili, Z.P. Li, and R.L. Workman, **PRC** **65**, 065204 (2002);

Q. Z., B. Saghai and Z.P. Li, **JPG** **28**, 1293 (2002);

X.H. Zhong, Q. Z., J. He, and B. Saghai, **PRC** **76**, 065205 (2007)

X.H. Zhong and Q. Z., arXiv:0811.4212, **PRC****79**, 045202(2009)

Thanks !

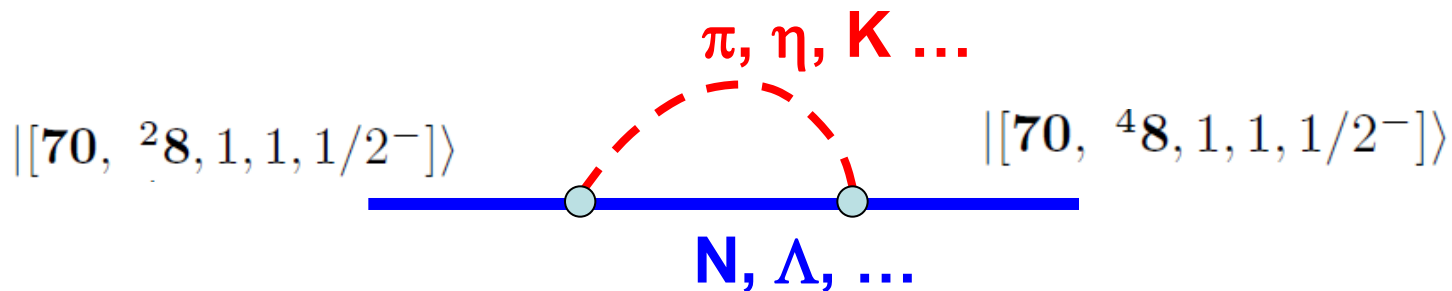
◆ A revisit to the S-wave state mixing

The mixing between pure $[70, {}^28]$ and $[70, {}^48]$ states is defined as

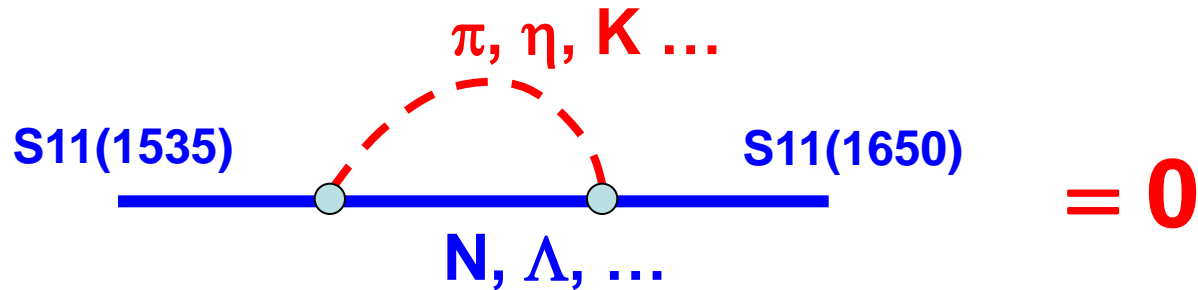
$$\begin{pmatrix} S_{11}(1535) \\ S_{11}(1650) \end{pmatrix} = \begin{pmatrix} \cos \theta_S & -\sin \theta_S \\ \sin \theta_S & \cos \theta_S \end{pmatrix} \begin{pmatrix} |[70, {}^28, 1, 1, 1/2^-]\rangle \\ |[70, {}^48, 1, 1, 1/2^-]\rangle \end{pmatrix}$$

Similarly, the D -wave mixing can be written as

$$\begin{pmatrix} D_{13}(1520) \\ D_{13}(1700) \end{pmatrix} = \begin{pmatrix} \cos \theta_D & -\sin \theta_D \\ \sin \theta_D & \cos \theta_D \end{pmatrix} \begin{pmatrix} |[70, {}^28, 1, 1, 3/2^-]\rangle \\ |[70, {}^48, 1, 1, 3/2^-]\rangle \end{pmatrix}$$



The physical states should be orthogonal which means:



This expectation can be examined by the K-matrix propagator between $[70, ^2 8]$ and $[70, ^4 8]$ mixing states:

$$G = \frac{1}{D_a D_b - |D_{ab}|^2} \begin{pmatrix} D_a & D_{ab} \\ D_{ab} & D_b \end{pmatrix}$$

$$\left\{ \begin{array}{l} D_a = s - m_a^2 + i\sqrt{s} \Gamma^a(s) \\ D_b = s - m_b^2 + i\sqrt{s} \Gamma^b(s) \end{array} \right. \quad \left\{ \begin{array}{l} \Gamma^a(s) = \Gamma_{\pi N}^a + \Gamma_{\eta N}^a + \dots, \\ \Gamma^b(s) = \Gamma_{\pi N}^b + \Gamma_{\eta N}^b + \dots. \end{array} \right.$$

$$D_{ab} \simeq \frac{i}{16\pi} [\rho_{\pi N} g_{S_{11}N\pi}^a g_{S_{11}N\pi}^b + \rho_{\eta N} g_{S_{11}N\eta}^a g_{S_{11}N\eta}^b]$$

Recalling that

$$H_m^{NR} = \sum_j \left\{ \frac{\omega_m}{E_f + M_f} \right\}$$

The $N^* \rightarrow NM$ tra

$$\alpha \equiv \langle \psi_{000}^s | q e^{i\sqrt{\frac{2}{3}}q\lambda_z} | \psi_{110}^\lambda \rangle = i \frac{q^2}{\sqrt{3}\alpha_h} e^{-q^2/6\alpha_h^2},$$

$$\begin{aligned} \beta &\equiv \langle \psi_{000}^s | e^{i\sqrt{\frac{2}{3}}q\lambda_z} \hat{p}_{3-} | \psi_{111}^\lambda \rangle = -\langle \psi_{000}^s | e^{i\sqrt{\frac{2}{3}}q\lambda_z} \hat{p}_{3+} | \psi_{11-1}^\lambda \rangle \\ &= -i\sqrt{\frac{2}{3}}\alpha_h e^{-q^2/6\alpha_h^2}, \end{aligned}$$

$$\gamma \equiv \langle \psi_{000}^s | e^{i\sqrt{\frac{2}{3}}q\lambda_z} \hat{p}_{3z} | \psi_{110}^\lambda \rangle = i \frac{\alpha_h}{\sqrt{3}} \left(1 + \frac{q^2}{3\alpha_h^2} \right) e^{-q^2/6\alpha_h^2},$$

$$\left\{ \begin{aligned} \mathcal{M}_{S_{11} \rightarrow NM} &= \frac{1}{f_m} [C_1 \langle \hat{H}_1 \rangle \alpha(q) + C_2 \langle \hat{H}_2 \rangle (\gamma(q) - \sqrt{2}\beta(q))], \\ \mathcal{M}_{D_{13}(D_{15}) \rightarrow NM} &= \frac{1}{f_m} \left[C_1 \langle \hat{H}_1 \rangle \alpha(q) + C_2 \langle \hat{H}_2 \rangle \left(\gamma(q) + \frac{\beta(q)}{\sqrt{2}} \right) \right] \end{aligned} \right.$$

with $C_1 \equiv -3 \left(\frac{\omega_m}{E_f + M_f} + 1 \right), \quad C_2 \equiv \frac{3\omega_m}{2\mu_q}.$

$\hat{H}_1(\alpha), \hat{H}_2(\gamma - \sqrt{2}\beta)$	$S_{11}^+ \rightarrow \Lambda K^+$	$S_{11}^+ \rightarrow p\eta$	$S_{11}^+ \rightarrow n\pi^+$	$S_{11}^+ \rightarrow p\pi^0$	$S_{11}^+ \rightarrow \Sigma^+ K^0$
$\langle N, J_z = \frac{1}{2} \hat{H}_1 S_{11}^+, J_z = \frac{1}{2} \rangle$	$-\frac{1}{6}$	$-\frac{\cos\theta}{3\sqrt{3}}$	$-\frac{2\sqrt{2}}{9\sqrt{3}}$	$\frac{2}{9\sqrt{3}}$	$-\frac{1}{9\sqrt{6}}$
$\langle N, J_z = \frac{1}{2} \hat{H}_2 S_{11}^+, J_z = \frac{1}{2} \rangle$	$-\frac{1}{6}$	$-\frac{\cos\theta}{3\sqrt{3}}$	$-\frac{2\sqrt{2}}{9\sqrt{3}}$	$\frac{2}{9\sqrt{3}}$	$-\frac{1}{9\sqrt{6}}$

We can then extract the N^*NM form factors given by the chiral effective Lagrangian in the NRCQM, e.g.

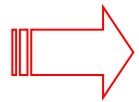
$$\sum_{spin} |\mathcal{M}_{hadron}|^2 \equiv (E_i + M_i)(E_f + M_f) \sum_{spin} |\mathcal{M}_{quark}|^2,$$

where

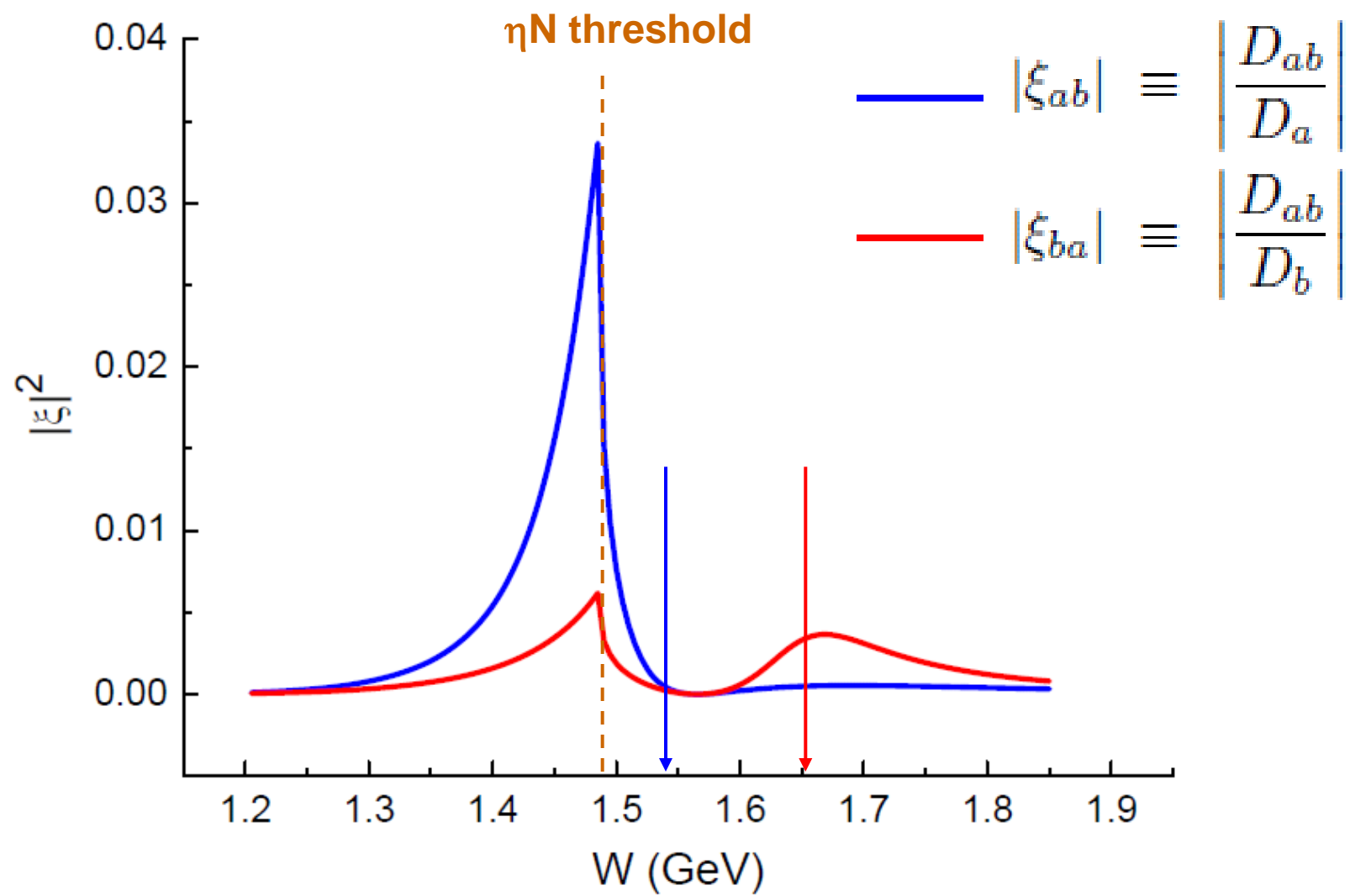
$$N^*(S_{11} \rightarrow NM) : \quad \mathcal{M}_{hadron}^{S_{11}} = g_{S_{11}NM} \bar{u}_N u_R,$$

$$N^*(D_{13} \rightarrow NM) : \quad \mathcal{M}_{hadron}^{D_{13}} = g_{D_{13}NM} \bar{u}_N \gamma_5 \gamma_\mu u_{R\nu} p_M^\mu p_M^\nu,$$

$$N^*(D_{15} \rightarrow NM) : \quad \mathcal{M}_{hadron}^{D_{15}} = g_{D_{15}NM} \bar{u}_N u_{R\mu\nu} p_M^\mu p_M^\nu,$$



$$\left\{ \begin{array}{l} \mathcal{M}_{quark}^{S_{11}} = \frac{1}{f_m} [C_1 \alpha(q) + C_2 (\gamma(q) - \sqrt{2} \beta(q))] \langle \hat{H} \rangle \\ \quad = \frac{1}{f_m} \frac{i \alpha_h e^{-q^2/6\alpha^2}}{\sqrt{3}} \left[C_1 \frac{q^2}{\alpha_h^2} + C_2 \left(3 + \frac{q^2}{3\alpha_h^2} \right) \right] \langle \hat{H} \rangle, \\ \mathcal{M}_{quark}^{D_{13}/D_{15}} = \frac{1}{f_m} [C_1 \alpha(q) + C_2 (\gamma(q) + \frac{\beta(q)}{\sqrt{2}})] \langle \hat{H} \rangle \\ \quad = \frac{1}{f_m} \frac{i q^2 e^{-q^2/6\alpha^2}}{3\sqrt{3}\alpha_h} \langle \hat{H} \rangle, \end{array} \right.$$



With the data for $S_{11} \rightarrow N\pi$ and $N\eta$ [1], i.e.

$$Br(S_{11}(1535) \rightarrow N\pi) = 35 \sim 55\%$$

$$Br(S_{11}(1650) \rightarrow N\pi) = 60 \sim 95\% ,$$

$$Br(S_{11}(1535) \rightarrow N\eta) = 45 \sim 60\%$$

$$Br(S_{11}(1650) \rightarrow N\eta) = 3 \sim 10\% ,$$



$$\theta_S \approx 24.6^\circ \sim 32.1^\circ$$

$$\theta_S^{OPE} = 25.5^\circ$$

$$\theta_S^{OGE} = -32^\circ$$

Similarly, with the data for $D_{13} \rightarrow N\pi$

$$Br(D_{13}(1520) \rightarrow N\pi) = 55 \sim 65\%$$

$$Br(D_{13}(1700) \rightarrow N\pi) = 5 \sim 15\% ,$$

$$Br(D_{13}(1520) \rightarrow N\eta) = 0.23 \pm 0.04\%$$

$$Br(D_{13}(1700) \rightarrow N\eta) = 0.0 \pm 1.0\% ,$$



$$\theta_D \approx 6.3^\circ \sim 18.3^\circ .$$

$$\theta_D^{OPE} = -52.7^\circ$$

$$\theta_D^{OGE} = 6^\circ$$

Relative signs for the N^*NM couplings are given by the NRCQM

$\theta_S(24.6^\circ \sim 32.1^\circ)$	$S_{11}^+ \rightarrow p\eta$	$S_{11}^+ \rightarrow \Lambda K^+$	$S_{11}^+ \rightarrow n\pi^+$	$S_{11}^+ \rightarrow p\pi^0$	$S_{11}^+ \rightarrow \Sigma^+ K^0$
$\mathcal{M}_{N^* \rightarrow NM}$	6.86 \sim 7.18	4.32 \sim 4.07	3.29 \sim 2.68	-2.312 \sim -1.92	3.32 \sim 3.88
$g_{S_{11}NM}$	7.03 \sim 7.35	4.42 \sim 4.16	3.37 \sim 2.74	-2.38 \sim -1.94	3.41 \sim 3.99
$g_{S_{11}NM}/g_{S_{11}p\eta}$	1	0.63 \sim 0.57	0.48 \sim 0.37	-0.34 \sim -0.27	0.49 \sim 0.54

TABLE VI: Strong coupling constants for $S_{11}(1535) \rightarrow NM$.

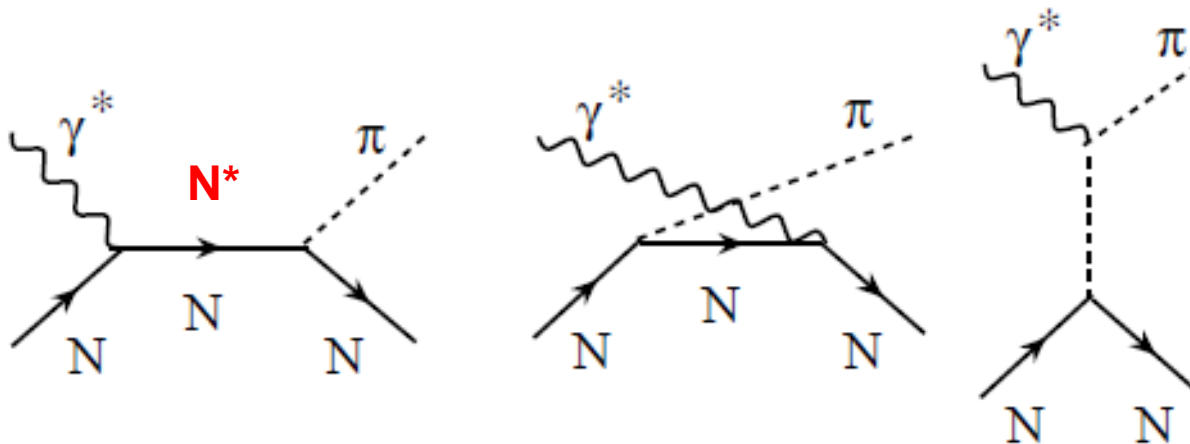
$\theta_S(24.6^\circ \sim 32.1^\circ)$	$S_{11}^+ \rightarrow p\eta$	$S_{11}^+ \rightarrow \Lambda K^+$	$S_{11}^+ \rightarrow n\pi^+$	$S_{11}^+ \rightarrow p\pi^0$	$S_{11}^+ \rightarrow \Sigma^+ K^0$
$\mathcal{M}_{N^* \rightarrow NM}$	-2.56 \sim -1.67	2.0 \sim 2.57	4.06 \sim 4.44	-2.85 \sim -3.15	-4.19 \sim -3.75
$g_{S_{11}NM}$	-2.50 \sim -1.63	1.96 \sim 2.51	3.96 \sim 4.34	-2.80 \sim -3.07	-4.0 \sim -3.58
$g_{S_{11}NM}/g_{S_{11}p\eta}$	1	-0.78 \sim -1.54	-1.58 \sim -2.66	1.12 \sim 1.88	1.6 \sim 2.2

TABLE VII: Strong coupling constants for $S_{11}(1650) \rightarrow NM$.

Indication of a destructive sign between $S_{11}(1535)$ and $S_{11}(1650)$ amplitudes in $\gamma p \rightarrow \eta p$, and $\pi^- p \rightarrow \eta n$.

arXiv: 0810.0997[nucl-th] by Aznauryan, Burkert and Lee.

It is important to have a correct definition of the common sign of amplitudes and relative sign between helicity amplitudes, i.e. $A_{1/2}$, $A_{3/2}$, and $S_{1/2}$.

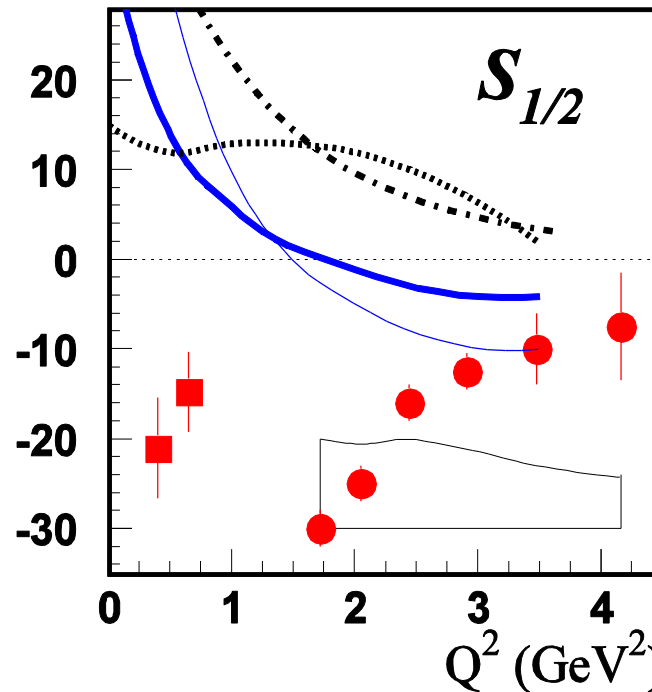
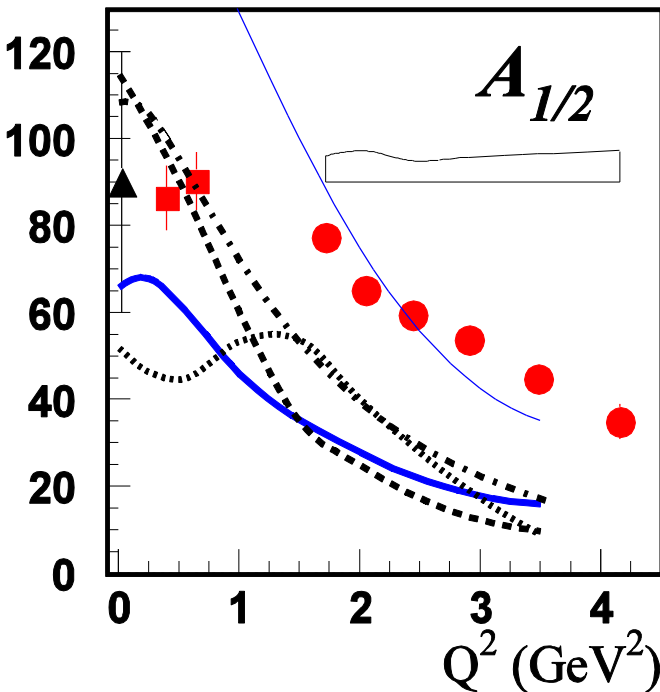


$\mathcal{A}_{1/2}$, $\mathcal{A}_{3/2}$, $\mathcal{S}_{1/2}$:

$$A_{\frac{1}{2}, \frac{3}{2}} = \zeta \mathcal{A}_{\frac{1}{2}, \frac{3}{2}}, \quad S_{\frac{1}{2}} = \zeta \mathcal{S}_{\frac{1}{2}}.$$

$$\zeta = -\text{sign}(g^*/g)$$

$\gamma^*p \rightarrow S_{11}(1535)$: 3q picture



Opposite sign
of $S_{1/2}$!!!

Impossible to change
in quark model !!!



LF RQM:

— Capstick, Keister,
PR D51 (1995) 3598
— Pace, Simula et al.,
PR D51 (1995) 3598

Combined with the difficulties
in the description of large width
of $S_{11}(1535) \rightarrow \eta N$ and large
 $S_{11}(1535) \rightarrow \phi N, \Lambda K$ couplings,
this shows that 3q picture for
 $S_{11}(1535)$ should be complemented

From I. Aznauryan, Electromagnetic N-N
Transition Form Factors Workshop, 2008*

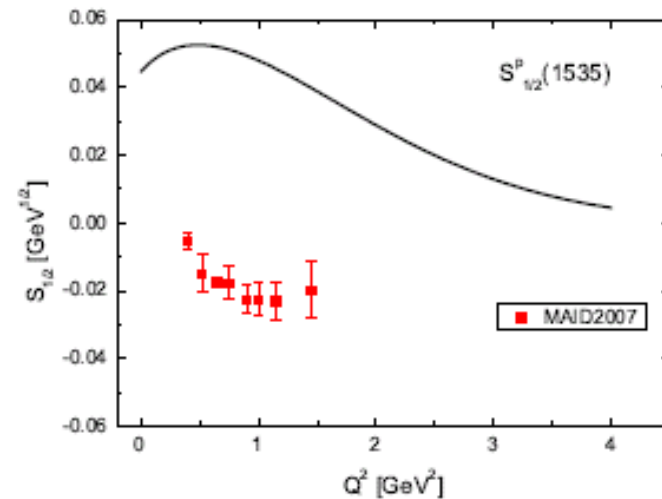
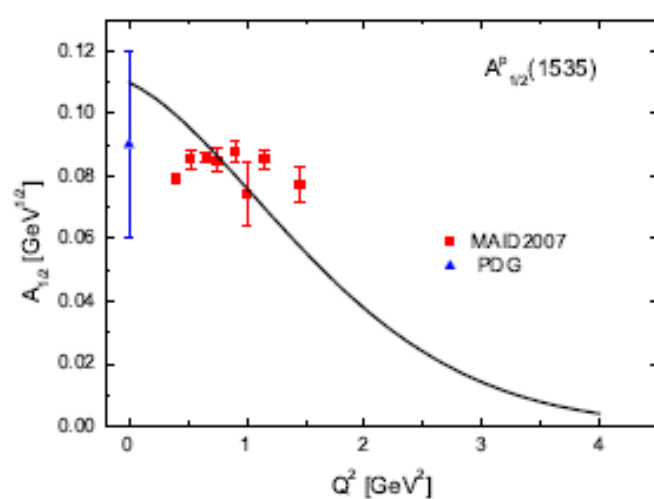


FIG. 1: Helicity amplitude for $\gamma^* p \rightarrow S_{11}(1535)$

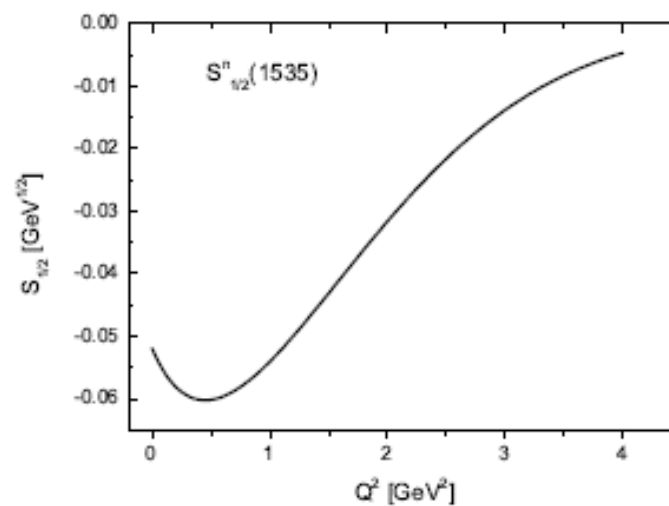
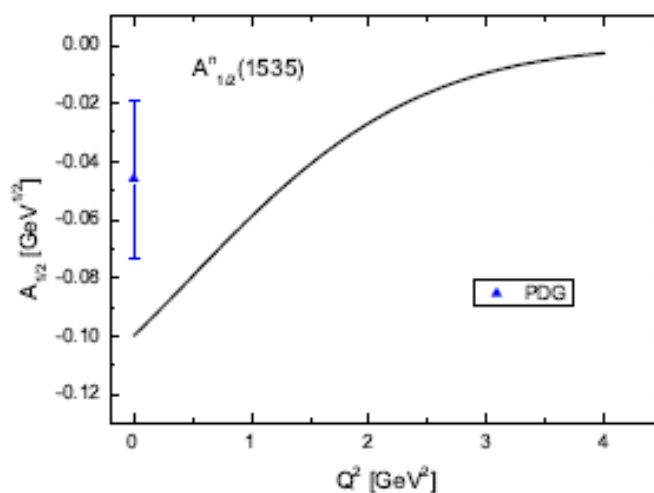


FIG. 2: Helicity amplitude for $\gamma^* n \rightarrow S_{11}(1535)$

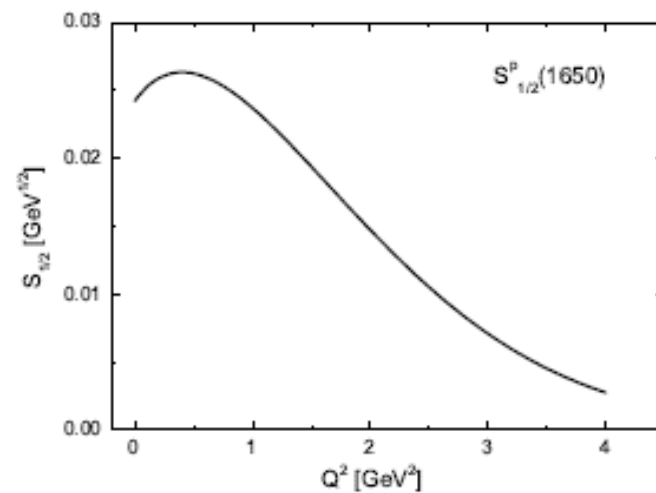
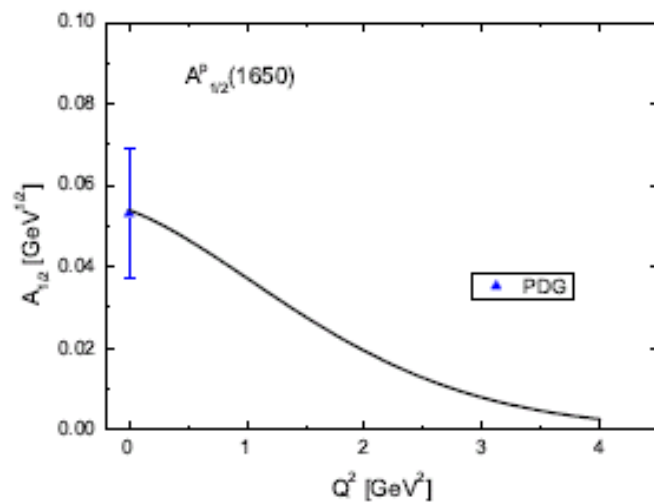


FIG. 3: Helicity amplitude for $\gamma^* p \rightarrow S_{11}(1650)$

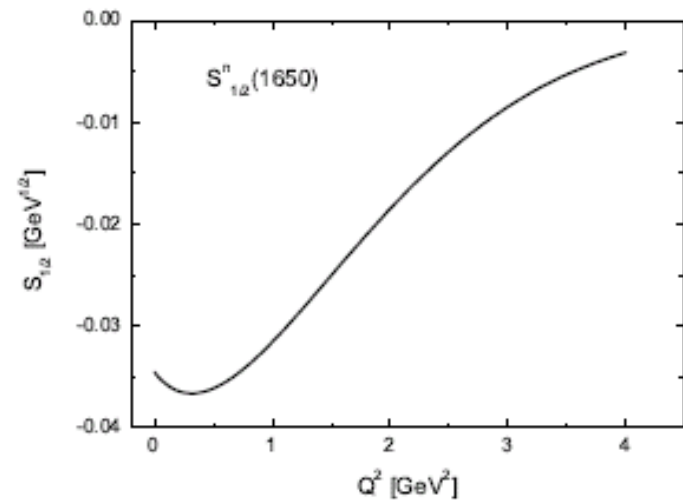
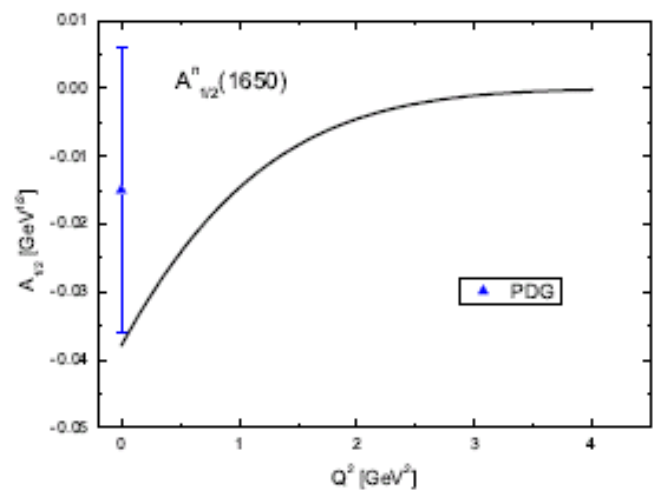


FIG. 4: Helicity amplitude for $\gamma^* n \rightarrow S_{11}(1650)$